Verifiable Advice to a Biased Policymaker^{*}

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Abstract

We develop a model of verifiable communication between a biased policymaker and a bureaucratic agency that has a preference for maintaining the status quo. We show that, in the absence of additional utility pressures on the agency, an increase in the policymaker's bias, which increases the distance between the policymaker's and the agency's ideal points, leads the agency to disclose more information. A key intuition for this result is that, in equilibrium, the lack of a revealing message from the agency functions as a signal to the policymaker that credibly compels her to choose more radical policies, with the agency being forced to reveal in order to hold back the policy radicalism. We also show that, while introducing the possibility of a utility bonus for revelation results in increased agency revelation, it can reverse the positive effect of the policymaker's bias on revelation and hinder the disclosure of additional information to more biased policymakers. Finally, we demonstrate that the higher bias of the policymaker exacerbates the asymmetry in the agency's revelation strategy, creating the appearance of ideological conflict with the policymaker.

Introduction

Elected officials coming from extreme ends of the political spectrum frequently invoke the language of "deep state" to complain about the resistance of civil servants and other state bureaucrats to their efforts to move the policy away from the status quo. The complaints are, of course, not entirely unfounded, since bureaucrats tend to have preferences for upholding the status quo (Peter; Ginsburg and Huq), and operate with a certain degree of

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informational and executive autonomy. But the interactions between them and the policymakers take place in a strategic environment, and the preference for different policy should not unproblematically be assumed to translate into choices.

We develop a strategic model of communication and policy-making that sheds new light on the effects of policy-maker bias on strategic information revelation from an agency. In the game we analyze, a bureaucratic agency with conservative – i.e., status-quo favoring – preferences has access to superior information about the state of the world than does the policy-maker. It chooses whether to reveal this information (send a verifiable message) to the policy-maker who prefers to tailor the policy choice to the state of the world but has a known directional bias. We detail the implications of two distinct pathways by which policymaker's bias affects the agency's revelation strategy: First, and more intuitively, greater policymaker bias makes the agency more reluctant to share information that reinforces the policymaker's bias and would prompt the policymaker to choose more extreme policy; however, by the same token, it is more willing to share information contrary to the policymaker's bias that might temper the policymaker's choice. Second, and more subtly, the policymaker's bias alters the default policy that the policymaker chooses in the absence of information revelation, which, in turn, affects the agency's decision to reveal.

Our first key result shows that when the agency's incentives to reveal information are induced by policy consequences, greater bias of the policy-maker strictly increases information revelation from the agency. To see the basic logic, suppose, without loss of generality, that the policy-maker has a right-ward bias. The agency will, then, want to reveal to her states of the world that pull the policy back to the left. It is straightforward that the states that would be revealed would include leftward states that the agency would never reveal to a more neutral policy-maker. But, and for the same reason, they will include some relatively right states as well: conditional on no revelation, the policy-maker anticipates that the state must be fairly far to the right, and the agency will wish to reveal its signal to the policy-maker to convince her that her guess is, in fact, too extreme.

We then study how the relationship between the policy-makers' bias and equilibrium revelation depends on two factors that may complicate the communication environment: the introduction of office-based utility for the agency (which may be manipulated by the policy-maker to help induce revelation) and the possibility of the agency's having statedependent preferences with varying degrees of status-quo oriented conservatism. We show that the central comparative static- that greater bias of the policy-maker leads to greater revelation from the agency- continues to hold in the presence of these factors for substantial parts of the parameter space. However, the possibility of office benefits for the agency leads to another surprising result: While greater such benefits directly promote revelation in equilibrium, they undermine the indirect effect of policymaker bias via chosen default policy, so that when the agency's office benefits are large enough, the agency's informational incentive to reveal its signal disappears because the policy-maker's expectation of what the state must be conditional on no revelation becomes sufficiently close to the policy chosen in the absence of revelation. The policy-maker bias has a positive effect on agency revelation when the agency's preferences are sufficiently conservative in valuing the status quo, but it flips when the agency's preferences become sufficiently responsive to the state.

Among other implications, the overall logic of the results offers a novel perspective on policy-makers' complaints of a "deep-state." Bureaucracies play a number of roles in the policy-making process, including providing information to policy-makers. Focusing on the informational role of bureaucracies and setting aside implementation, our analysis suggests that policymakers with well-defined policy biases should, indeed, expect to receive asymmetric patterns of bureaucratic advice, tilted against their ideologically preferred direction. However, despite that asymmetry, the information a more biased policy-maker receives from a status-quo oriented bureaucracy may be better, not worse, than the information that a less biased policy-maker would receive. In other words, as far as the provision of information is concerned, complaints about the "deep state" should be taken with a fair amount of skepticism.

Connection to the Literature

Delegation and communication within hierarchies has been a focus of a substantial body of political economy scholarship (for reviews, see Gailmard and Patty (2012) and Sobel (2013)). One branch of this scholarship models communication as "cheap talk" in which bureaucrats' potential messages are not directly constrained by their information (Crawford and Sobel (1982); Gilligan and Krehbiel (1989); Austen-Smith (1990); Austen-Smith (1993)). A key finding of this literature is that divergence in the actors' preferences curtails communication, and successful communication at all occurs only when the advisor's and the policymaker's preferences are sufficiently aligned. An important exception relevant for our analysis is Callander (2008), which studies an expert bureaucrat's advice to a legislator in an environment in which the bureaucrat's private information from the advice. Callander shows that, in the absence of an institutionalized commitment to implement the received advice, greater divergence in primitive preferences between bureaucrat and legislator sometimes induces greater voluntary delegation of policy-making powers from the legislator to the bureaucrat. This suggests a certain affinity with our result that greater preference divergence spurs more information revelation. The mechanisms producing these results are, however, very different.¹

A second branch of this scholarship models the communication of verifiable information. A key result in this literature is that all private information is revealed in equilibrium (Milgrom (1981), Milgrom (2008)). In the model we study, the agency's messages consist of hard evidence, but nonetheless the agency does not disclose everything. Since Milgrom (1981), important subsequent works study conditions under which the unraveling logic of full disclosure does not hold. This includes Shin (1994), which shows that the policymaker will not be able to infer perfectly the advisor's private information in the event of "no news" when the advisor's knowledge is imperfect; see also Wolinsky (2003). Dziuda (2011) shows that, in a setting where the fixed expert's preferences are different and unknown to the decisionmaker, there is never full disclosure, but the expert offers pros and cons for the advocated alternative in order to pool with the honest/non-strategic type. While in our model, there is never full disclosure either, the unraveling logic is an important element of the mechanism underlying our results: because in the absence of disclosure, the policy-maker assumes that the state must be too extreme for the bureaucrat, the policy-maker chooses a more extreme policy, which lessens the incentives to withhold information.

Denisenko, Hafer and Landa (2022) study the transmission of verifiable information between a sender of known competence with preference for the status-quo and a neutral receiver who wishes to match the state of the world. They show that less competent senders have stronger incentives to reveal their information to the policymaker than more competent ones, inducing a trade-off between the quality of advice the sender receives and the likelihood of receiving it. In contrast with that model, we abstract away from variation in sender competence and introduce the bias of the receiver to focus our analysis on its effects on information transmission.

Add discussion of Bhattacharya and Mukherjee (2013), Lipnowski and Ravid (2020), Che and Kartik (2009), Patty (2009), Kartik (2009).

The General Environment

We analyze a strategic interaction between a Policymaker (she) and an Agency (it). The Policymaker wishes to implement a policy that will match the state of the world and accomplish her partisan agenda; these goals may be in tension. The Policymaker does not directly observe the state of the world and must, instead, obtain relevant policy information via the

¹A different exception, farther afield, is Battaglini (2002), which shows that the receiver may obtain full revelation when there are multiple senders.

recommendation released by the Agency. The timeline of the game is as follows:

- 1. Nature determines the state of the world $w \in \mathbf{R}$, where w is a draw from a standard normal distribution N(0, 1).
- 2. The Advisor observes a signal s about the state of the world $w, s = w + \varepsilon$. The variable ε represents random noise drawn from a standard normal distribution, $\varepsilon \sim N(0, 1)$.
- 3. The Advisor chooses whether to send (verifiable) message m = s to the Policymaker, $m \in \{s, \emptyset\}.$
- 4. The Policymaker observes message m and decides which policy $a \in \mathbf{R}$ to implement.

The Policymaker wants to choose policy a to best satisfy her partial bias b and to best match the state of the world. These goals are in tension:

$$U_L(a|b) = -(w-a)^2 + b \cdot a.$$
 (1)

When bias b is positive the Policymaker has a rightward bias, which implies that she benefits when she implements policies to the right of the status quo. When b is negative, the Policymaker, instead, exhibits a *leftward bias* and is tempted to implement left-leaning policies. In what follows, we assume that b > 0, meaning the Policymaker exhibits a rightward bias. (The case b < 0 is symmetric to this one.)

The Agency's inclinations differ from those of the Policymaker. We assume the agency to be conservative in its preference and dislike any policy change, with increasing marginal losses. The Agency's utility is

$$U_A(m|b) = -a(m)^2.$$
 (2)

We will refer to the Agency's message m = s as the *revealing* message. Conditional on receiving such a message from the Agency, the Policymaker rationally updates her belief about the state of the world $E[w|m] = \frac{m}{2}$ and, thus, implements optimal policy $a^*(m) = \frac{m}{2} + \frac{b}{2}$. Likewise, the Policymaker updates her belief about w when she does not receive the revealing message $(m = \emptyset)$; we denote the optimal default policy the Policymaker implements after message $m = \emptyset$ as $d^*(b)$.

The Agency, in turn, chooses its revelation strategy optimally, taking into account the Policymaker's policy response. The following proposition characterizes the Agency's and the Policymaker's equilibrium strategies **Proposition 1.** In equilibrium, the Agency reveals the signal it observes if and only if $s \in [\underline{s}^*(\cdot), \overline{s^*}(\cdot)]$, where

$$\frac{s^{*}(b) \equiv -2 \cdot \underbrace{d^{*}(b)}_{\substack{\text{Indirect Effect}\\ of Bias on s^{*}}} - \underbrace{b}_{\substack{\text{Direct Effect}\\ of Bias on s^{*}}}, \\
\overline{s^{*}}(b) \equiv 2 \cdot \underbrace{d^{*}(b)}_{\substack{\text{Indirect Effect}\\ of Bias on s^{*}}} - \underbrace{b}_{\substack{\text{Direct Effect}\\ of Bias on s^{*}}}, \\$$
(3)

and $d^*(b)$ solves

$$d = b/2 + \frac{1}{\sqrt{\pi}} \cdot \left(e^{-(b/2-d)^2} - e^{-(b/2+d)^2}\right).$$
(4)

The Policymaker implements policy $a^*(m) = \frac{m}{2} + \frac{b}{2}$ if the Agency reveals s and chooses policy $d^*(b)$ when the Agency does not $(m = \emptyset)$.

Proof. Appendix A.

The Policymaker's bias exerts two effects on the Agency's revelation strategy. The *direct* effect of the bias, deriving from the Policymaker's policy response to the revelation of s, shifts the Agency's revelation thresholds in the direction opposite to the Policymaker's bias.

The second, *indirect*, effect of the Policymaker's bias on the Agency's strategy occurs via the Policymaker's policy choice when she does not receive a revealing message, $d^*(b)$. Figure 1a shows the decomposition of the impact of the Policymaker's bias on the Agency's strategy as a function of bias b. The dashed horizontal line in Figure 1a represents a benchmark of the Agency's revelation with the unbiased Policymaker. The dash-dotted line depicts the shift of the Agency's revelation interval driven by the direct effect of the bias, holding fixed the default policy. Finally, the solid orange curves represent the equilibrium revelation thresholds, reflecting both the direct and indirect effects of the bias.

Figure 1: Impact of the Policymaker's Rightward Bias (b > 0) on the Agency's Revelation Strategy.



(a) The Agency's Revelation Strategy as a Function of the Policymaker's Bias (b).



(b) The Optimal Default Policy as a Function of the Policymaker's Bias (b).

In the absence of revelation, the Policymaker chooses default policy $d^*(\cdot)$ that solves

$$d = \underbrace{b/2}_{\substack{\text{Direct Effect}\\ of Bias on d^*}} + \underbrace{\frac{1}{\sqrt{\pi}} \left(e^{-(b/2-d)^2} - e^{-(b/2+d)^2}\right)}_{\substack{\text{Indirect Effect}\\ of Bias on d^*}}.$$
(5)

Lemma 1. Optimal default policy $d^*(\cdot)$ always exceeds b/2 when the Policymaker's bias is positive and is less than b/2 otherwise.

Proof. See Appendix B.

The optimal default policy the Policymaker sets is similarly affected by the Policymaker's bias. We can separate two distinct effects. Keeping the Agency's revelation strategy fixed, the higher the Policymaker's bias, the more she benefits when she implements policies coaligned with her bias. Thus, in the absence of the revealing signal, the default policy the Policymaker chooses shifts in the direction of her bias. At the same time, a biased Policymaker should infer that the information the Agency is concealing is more likely to be co-aligned with her bias than not. This further encourages the Policymaker to adopt policies that confirm her bias in the absence of information. To distinguish between the two outlined mechanisms by which the bias affects the optimal default policies, we denote the former one the *direct effect of bias on d*^{*} and the second one the *indirect effect of bias on d*^{*} in equation 4. Figure 1b depicts the optimal default policy (d^*) as a function of the Policymaker's bias when only the *direct effect of bias on d*^{*} is included and when both effects are included. Because both effects of the bias on the optimal default policy are co-aligned, we can state the following result:

Proposition 2. The optimal default policy (d^*) , which the Policymaker implements when the Agency does not reveal s, increases in the Policymaker's bias (b).

Proof. See Appendix C.

Overall, the higher is the Policymaker's policy bias, the more extreme policies the Policymaker chooses in the absence of an informative recommendation (message) from the Agency. Because of that, the marginal opportunity cost of information revelation decreases in the Policymaker's bias, which encourages the Agency to conceal less from the Policymaker.

The following two propositions summarize the impact of the Policymaker's bias on the Agency's revelation strategy.

Proposition 3. For any value of the Policymaker's bias (b),

- 1. the Agency reveals more information on the side opposite the Policymaker's bias than on the side co-aligned with the Policymaker's bias: for any b > 0, $|\underline{s^*}(b)| \ge |\overline{s^*}(b)|$;
- 2. the asymmetry in the Advisor's revelation increases in the Policymaker's bias: for any $b > 0, |\underline{s^*}(b)| |\overline{s^*}(b)|$ increases in b.

Proof. See Appendix D.

The direct and indirect effects of the Policymaker's bias on the revelation thresholds are mutually reinforcing when it comes to the threshold opposite the bias (e.g., the impact of the rightward bias on the left-leaning signals) but are in tension for the threshold on the same side as the bias.

For a Policymaker with a rightward bias (b > 0), when it comes to the left-leaning (negative) signal, the direct effect of an increase in the bias shifts the left threshold leftward, and the indirect effect pushes it further leftward. However, when it comes to the right-leaning (positive) signals, the direct and indirect effects of the bias run counter to each other – the direct effect shifts the right threshold to the left, while the indirect effect pushes it to the right. Note that, as the Agency seeks to counteract the biased Policymaker's preference, the biased Policymaker always gets relatively less advice urging policies consistent with her bias and relatively more advice urging policies contrary to her bias, and this asymmetry worsens as the bias increases. While it might appear that the Agency systematically seeks to thwart the Policymaker's agenda or has preferences diametrically opposed to her (cue the former President's complaints about the "deep state"), a different interpretation here is that it is the Policymaker.

Before stating our next result, we introduce an additional definition. We will say that equilibrium communication is more informative for parameter value x' than for parameter value x'' if every signal that Agency reveals at value x'', it will also reveal at value x', and there are additional signals it reveals in the latter case that it does not reveal in the former, i.e., $[\underline{s}^*(x''; \cdot), \overline{s}^*(x''; \cdot)] \subset [\underline{s}^*(x'; \cdot), \overline{s}^*(x'; \cdot)].$

Proposition 4. The higher is the Policymaker's bias (b), the more informative equilibrium communication between the Policymaker and the Agency becomes.

Proof. See Appendix E.

It is important to note that lack of revelation remains communicative and informs the Policymaker's inferences about the state of the world. Proposition 4, thus, highlights that the Policymaker's bias improves the informativeness of communication between the Policymaker and the Agency both when revelation occurs and when the Agency conceals its information. This result might seem surprising as it runs counter to general predictions of the cheaptalk literature: when communication is costless and unverifiable, a greater gap between the sender's and the receiver's preferences inevitably lowers the quality of advice (Crawford and Sobel 1982). We demonstrate that, in contrast, verifiable information settings may produce the opposite result. Despite the highlighted tension between the direct and indirect effects of the bias on the revelation strategy, the Policymaker's bias encourages the Agency to reveal strictly more signals when the Agency is driven by the desire to retain the status-quo policy.

To disentangle the impact of the Policymaker's bias on the Agency's revelation, begin by assuming the Policymaker to be unbiased. In equilibrium, the Agency never reveals to the unbiased Policymaker signals different from the status quo: $\overline{s}^*(b=0) = \underline{s}^*(b=0) = 0$. The unbiased Policymaker, correspondingly, believes that, in the absence of revelation, the expected value of the state w equals the status quo and implements it as a default policy: $d^*(b=0) = 0$. Holding the Agency's revelation strategy fixed, a Policymaker's higher bias does not alter the Policymaker's posterior beliefs but shifts the optimal default policy away from the status quo. Given that the default policy does not equal the status quo, the Agency, then, benefits from revealing to the Policymaker some information that counteracts her bias, with higher bias inducing more extreme advice. The skewed revelation, in turn, affects the inferences the Policymaker draws from the absence of advice $(m = \emptyset)$, shifting the optimal default policy, which causes the Agency to begin revealing even more signals, including co-aligned with the Policymaker's bias, to avoid drastic policy changes.

Figure 2 depicts the Agency's revelation strategy (solid orange curves), the range of policies the Policymaker implements when the Agency reveals s (solid blue shaded area), and the default policy (dashed blue curve) she chooses when she receives no message ($m = \emptyset$). The Policymaker's bias, thus, allows her to elicit more advice from the Agency despite not directly rewarding revelation or punishing the lack thereof.

Figure 2: Agency's Equilibrium Revelation Thresholds $(\overline{s^*}(b), and \underline{s^*}(b))$, the Implemented Policies Interval $(a^*(m))$, and the Default Policy $(d^*(b))$ as a Function of the Policymaker's Bias (b)



As described above, in this model, the Agency is restricted to messages m = s and $m = \emptyset$. It is natural to wonder, however, whether Proposition 4 would be robust to expanding the Agency's action set to allow for the possibility of strategies that could partially obscure the Agency's signal. Might the Agency find it advantageous to reveal some information about s without revealing s precisely? To consider this possibility, suppose that the signal space is partitioned into M (s.t. M > 1) convex intervals and that the Agency can send a message m to the Policymaker, such that $m \in \{\emptyset, m_1, m_2, ..., m_M\}$: a message $m = \emptyset$ represents a lack of revelation, while a message $m \neq \emptyset$ indicates that the Agency's signal s falls within a specific interval. Assume that this partition is common knowledge.

We can see now that when the Agency has the freedom to choose a partition, it cannot commit to anything other than the most precise partition available: When the Policymaker receives a message indicating that the Agency's signal falls within a particular partition, she forms a belief about the most likely state of the world and devises a policy that accounts for her bias and her belief. Given that M > 1, at least one message revealed by the Agency won't implement the Agency's most preferred policy and, instead, will result in a policy more extreme than what the Agency desires. However, this implies that there will always be a signal within the corresponding interval that the Agency would prefer to report directly, rather than sending the coarse message.

We can also address the robustness of Proposition 4 to the existence of exogenous constraints on the Agency's ability to reveal *s* with perfect precision: e.g., the Agency may only have a coarse understanding of the signals it observes, preventing it from sending messages it does not fully comprehend (Hagenbach and Koessler, 2020); language barriers between the sender and the receiver can limit the sender's ability to fully comprehend the intended message (Blume and Board, 2013); or there may exist external constraints on the Agency-Policymaker communication from the nature of the message exchange itself. We show in Appendix F (Proposition 9) that Proposition 4 is robust to this possibility of the Agency's messaging space being exogenously constrained to finite convex partitions of the signal space.

Office Benefit

Given the value to the Policymaker of the Agency's information, it is natural to consider the possibility that the Policymaker might induce revelation through rewards and punishments. In particular, the Policymaker might impose costs on the Agency for failing to reveal its information, including, but not limited to, higher levels of congressional scrutiny or the reduction of the Agency budgets (Balla 1998). To examine the effects of such inducements on equilibrium revelation, in this section we assume that the Agency receives a benefit R, which we call office benefit, when it shares its private information with the Policymaker. The Agency's utility, then, becomes

$$U_A(m|b,R) = \begin{cases} -a(m)^2 + R & \text{if } m \neq \emptyset \\ -a(m)^2 & \text{if } m = \emptyset. \end{cases}$$
(6)

The presence of the office benefit R does not affect the inferences the Policymaker makes when the Agency reveals its signal. Upon observing message m, the Policymaker implements policy $a^*(m) = \frac{m}{2} + \frac{b}{2}$. We denote the optimal default policy the Policymaker implements in the absence of revelation as $d^*(b, R)$. The next proposition characterizes the equilibrium strategy profile for the Agency and the Policymaker:

Proposition 5. In the equilibrium of the game with office benefit R, the Agency reveals

signal s when $s \in [\underline{s^*}(b, R), \overline{s^*}(b, R)]$ and conceals it otherwise, where

$$\underline{s^{*}}(b,R) \equiv -2 \cdot \sqrt{R} + \underbrace{d^{*}(b,R)^{2}}_{\substack{\text{Indirect Effect}\\ of the Bias on s^{*} \end{tabular}}} - \underbrace{b}_{\substack{\text{Direct Effect}\\ of the Bias on s^{*} \end{tabular}},$$

$$\overline{s^{*}}(b,R) \equiv 2 \cdot \sqrt{R} + \underbrace{d^{*}(b,R)^{2}}_{\substack{\text{Indirect Effect}\\ of the Bias on s^{*} \end{tabular}}} - \underbrace{b}_{\substack{\text{Direct Effect}\\ of the Bias on s^{*} \end{tabular}}},$$

$$(7)$$

and the optimal default policy $d^*(b, R)$ solves

$$d = \underbrace{b/2}_{\substack{\text{Direct Effect}\\ of Bias on \ d^*}} + \frac{1}{\sqrt{\pi}} \cdot \underbrace{\left(e^{-(b/2 - \sqrt{R+d^2})^2} - e^{-(b/2 + \sqrt{R+d^2})^2}\right)}_{\substack{\text{Indirect Effect}\\ of Bias on \ d^*}}.$$
(8)

The Policymaker implements policy $a^*(m) = \frac{m}{2} + \frac{b}{2}$ if she observes a revealing message, m = s, and chooses policy $d^*(b, R)$ otherwise.

Proof. See Appendix G.

Note that 7 and 8 evaluated at R = 0 yield the equilibrium of the main model, characterized in Proposition 1.

Proposition 6.

- 1. The higher the office benefit R, the more informative equilibrium communication between the Policymaker and the Agency becomes.
- 2. The informativeness of equilibrium communication is strictly increasing in the Policymaker's bias b iff

$$d^{*}(b,R)^{2} \cdot (4 \cdot (\frac{\partial d^{*}(b,R)}{\partial b})^{2} - 1) > R.$$
(9)

Proof. See Appendix H.

Figure 3: Impact of the Office Benefit R on the Agency's Revelation Thresholds



Figure 3 depicts the revelation thresholds the Agency adopts as the office benefit R increases. Higher office benefit induces the Agency to disclose more information to the Policymaker, widening the revelation interval.

The impact of the Policymaker's bias on the Agency's optimal conduct is akin to that observed in the baseline model. The *direct* effect of the bias shifts revelation in the opposite direction of the bias, while its *indirect* effect expands the extent of disclosure. The (rightward) bias always decreases the lower bound of revealed signals, i.e., it increases the disclosure of signals that run counter to the Policymaker's bias. Nevertheless, contrary to Proposition 4, the Policymaker's bias has a non-monotonic effect on the upper bound of the revelation interval.

The non-monotonic effect of the Policymaker's bias on the Agency's revelation thresholds is a result of the trade-off between the policy benefits and the office benefit. When the office benefit is present, the Agency's revelation serves a dual purpose. First, as in the baseline model, the Agency discloses information when such disclosure yields favorable policy outcomes, as perceived by the Agency, compared to the expected outcomes under the default policy. Second, the Agency reveals information to achieve the office benefit R.

In equilibrium, when the Policymaker's bias is small, the Agency discloses information primarily to obtain the office benefit R. The revelation thresholds, thus, remain balanced around the status quo. (The dashed line in Figure 3 illustrates the revelation interval as a function of R for b = 0.) This near symmetry implies that, in the absence of disclosure, the Policymaker's posterior belief corresponds to an expected value that neighbors the status quo. As the Policymaker's bias increases, however, the policies he implements with and without revelation from the Agency shift away from the status quo in the direction of the Policymaker's bias. Importantly, because the Agency's revelation is driven by its pursuit of the fixed gain R and its (quadratic) utility from policy, the farther the policies shift from the Agency's ideal point, the higher the office benefit it requires to compensate it for revelation of the marginal signal. Thus, for low values of bias b, and increase in b discourages the revelation of information co-aligned with the Policymaker's bias, decreasing the upper revelation threshold.

Note, however, that the same factors that discourage revelation of information co-aligned with the Policymaker's bias simultaneously encourage revelation of signals that oppose the bias. Higher bias, thus, induces asymmetry in the Agency's revelation strategy. Because of that asymmetry, concealment shifts the default policy further away from the status quo since the Policymaker updates in the direction of his bias when $m = \emptyset$. Now, as the Policymaker's bias increases, the Agency reveals information not only to gain the office benefit R, but also to prevent the realization of the default policy. The upper revelation threshold, thus, begins to increase in the Policymaker's bias b.

Lastly, it is important to note that the posterior the Policymaker forms, and, thus, the indirect effect of the bias on the default policy, is bounded. Even when the Agency only reveal signals that oppose the Policymaker's bias, the state of the world conditional on the lack of revelation never exceeds the threshold $\frac{1}{\sqrt{\pi}}$. At the same time, the direct effect of the bias is unbounded – it shifts implemented policies away from the status quo, decreasing the office benefit's value for the Agency and thus decreasing the Agency's incentives to reveal information. Figure 4 shows the Agency's revelation strategy as a function of the Policymaker's bias *b* in the presence of a positive office benefit. The solid orange line represents the Agency's upper bound on signals it will reveal. As described above, it first decreases in bias, then increases, and, finally, decreases in bias once again. In contrast, the lower revelation threshold strictly decreases in the Policymaker's bias.



Figure 4: Upper Revelation Threshold as a Function of the Policymaker's Bias

The dashed blue line in Figure 4 highlights the important benchmark of the Agency's revelation strategy with an unbiased Policymaker, for the same office benefit. It should be noted that in certain circumstances, policymakers with higher bias are privy to more informative communication than their unbiased counterparts. This disparity arises due to the Agency's efforts to circumvent the abrupt policy changes that follow failure to reveal *s*, much as in the baseline model. However, when the office benefit is significant, and the Agency's revelation serves to earn this benefit, mere policy objectives alone may not be compelling enough to encourage more disclosure. The next proposition characterizes conditions under which a more biased Policymaker will observe strictly more information than would an unbiased Policymaker.

Proposition 7. There exists a threshold $R^*(b)$ such that the Agency reveals strictly more information to the biased Policymaker than to the unbiased one when $R \in [0, R^*(b))$.

Proof. See Appendix I.

Figure 5 depicts the difference between the upper revelation threshold chosen by the Agency communicating with a biased Policymaker (b = 1) and the upper revelation threshold

chosen by the Agency when the Policymaker is unbiased. For bias b, this disparity is

$$I(b,R) \equiv \overline{s^*}(b,R) - \overline{s^*}(b=0,R).$$

When the office benefit is sufficiently low $(R < R^*(b))$, the Agency reveals strictly more information to a biased policymaker than to an unbiased one. However, as the office benefit (R) increases, the Agency is prompted to reassess the importance of its policy objectives vis-à-vis the value of the office benefit. When R is sufficiently high, greater bias shifts implemented policies away from the status quo, on the margin, and this deviation from the status quo prompts the Agency to demand a commensurately higher reward for disclosure.

Figure 5: Difference between Upper Revelation Threshold Introduced by the Agency with the Biased Policymaker $(\overline{s^*}(b, R))$ and the Agency with the Unbiased Policymaker $(\overline{s^*}(b = 0, R))$ as a Function of the Agency's Office Valuation (R)



While the presence of the office benefit directly improves communication between the Policymaker and the Agency, as seen in Figure 3, the revelation of certain signals requires no reward. For instance, the orange dashed-shaded area in Figure 6 shows signals the Agency reveals when R = 0. The blue solid-shaded areas show the communication improvement

that committing to directly rewarding revelation can purchase (assuming that revelation of any signal is rewarded).

Importantly, revelation under this conditional reward scheme does not differ from the one with unconditional reward. While in the context of our model it does not affect the Agency's nor the Policymaker's utilities, if the cost of the reward were to enter the Policymaker's objective function, conditional revelation presents a clear Pareto-improvement as it offers the same information at a lower cost.

Figure 6: Blue shaded area depict areas where revelation reward improves communication between the Policymaker and the Agency. The orange shaded area show the region where revelation occur regardless of the reward



Robustness to State-Dependence of Agency's Preferences

In the baseline model, two factors contribute to the misalignment of preferences between the Agency and the Policymaker. First, the Agency is assumed to be extremely conservative and,

thus, to prioritize the maintenance of the status quo, whereas the Policymaker favors policies that adapt to the current state of the world. Second, the Policymaker has a vested interest, which the Agency does not share, in implementing partian (biased) policies, irrespective of the state of the world.

In this section, we relax the first assumption, allowing the Agency's preferences to be state-dependent, to a degree. Formally, we assume the Agency's ideal policy is a weighted average of the state w and the status quo (0). In other words, the Agency wants to strike a balance between maintaining the status quo and aligning implemented policies with the state of the world. The Agency's utility is

$$U_A(a|c) = -(a - (1 - c) \cdot w)^2, \tag{10}$$

 \square

where $c \ (c \in [0, 1])$ measures the Agency's conservatism.

We obtain the following result:

Proposition 8. The Agency's revelation

- 1. strictly decreases in the Agency's conservatism, and
- 2. strictly increases in the Policymaker's bias when $c \ge 1/2$ and strictly decreases in the Policymaker's bias otherwise.

Proof. See Appendix J.

As the Agency becomes less conservative, i.e., as its preferences better align with those of the Policymaker, the Agency discloses more information to the Policymaker. Figure 7 depicts the Agency's revelation strategy as a function of its conservatism.

When the Agency discloses information opposite to the Policymaker's bias, the Policymaker implements policy less extreme than that which would fully match the state of the world. This policy moderation benefits the Agency, which balances matching the state of the world and maintaining the status quo. Lower conservatism, which corresponds to the Agency placing greater importance on matching the state of the world, encourages the revelation of information opposing the Policymaker's bias. The solid curve in Figure 7 shows how the extent of co-alignment between the Agency and the Policymaker influences the degree to which the Agency is incentivized to disclose information.

However, when the signal aligns with the Policymaker's partial bias, the Policymaker, if informed of the signal, implements a policy more extreme than that which would match the expected state of the world. In this case, the Agency discloses information because the adoption of the endogenously determined default policy would be even worse. The revelation strategy of the Agency with respect to signals that align with the Policymaker's bias is motivated by two factors. First, the Agency discloses information when the default policy is excessively extreme given the signal received. The dashed curve in Figure 7 illustrates how the Agency's conservatism influences its willingness to disclose information to counteract the implementation of extreme default policies. When c > 1/2, a decrease in the level of conservatism leads to an increase in the disclosure of information opposing the Policymaker's bias, which further drives the default policy in the direction of the Policymaker's bias, which further encourages the Agency to disclose information co-aligned with the Policymaker's bias.

Second, the Agency reveals information when the default policy is not extreme enough to account for necessary changes in policy. When c < 1/2, the Agency prioritizes matching the current state of the world over maintaining the status quo, and begins providing advice inducing more extreme policies, because, in some cases, the default policy is not sufficiently extreme to reflect adequately the realized state of the world. The dash-dotted curve in Figure 7 demarcates the revelation area in which the Agency discloses signals because the default policy is not sufficiently extreme. This area expands as the Agency's conservatism decreases, which then decreases the default policy when c < 1/2. Lowering the default policy, in turn, diminishes the possibility that the default policy is excessive for the state of the world, and which reduces the Agency's incentive to reveal information to counteract an excessive default policy.



Figure 7: Agency's Revelation as a Function of its Conservatism

The second part of Proposition 8 highlights that when the Agency's conservatism falls below a certain threshold (c < 1/2) the informativeness of the communication between the Policymaker and the Agency decreases in the Policymaker's bias, but increases when the Agency's conservatism is sufficiently high (c > 1/2). When the Agency is highly conservative (c > 1/2), the mechanism behind the bias's impact on revelation does not differ from that described in the baseline model. In the subsequent analysis, we focus on the case of low Agency conservatism.

When the Agency's conservatism is low (c < 1/2), the Agency reveals all signals inducing policies opposite to the Policymaker's bias. The impact of bias on revelation strategy is, therefore, only relevant when it concerns signals co-aligned with the Policymaker's bias. Figure 8 illustrates the Agency's revelation strategy as a function of the Policymaker's bias when c = 0. Low conservatism encourages the Agency to reveal signals co-aligned with the Policymaker's bias when the default policy is either excessively extreme given the observed signal (area below the solid curve in Figure 8) or not extreme enough (area above the dashed curve in Figure 8). Increasing Policymaker's bias induces implementation of policies more extreme than the Agency's ideal policy given the signal it observes. The Agency, thus, is less willing to reveal information that provokes more extreme policies than the default policy as the Policymaker's bias increases (the dashed curve in Figure 8 increases in bias b).

The change in the Agency's revelation strategy encourages the choice of a more extreme policy conditional on the lack of revelation, which has consequences like those described in the baseline model. In particular, increasing the default policy encourages the Agency to reveal more signals, namely those that produce policies less extreme than the default policy (the solid curve in Figure 8 increases in bias b). However, despite this increase, the communication between the Agency and the Policymaker becomes, overall, less informative as a function of bias when the Agency's conservatism is low, because the indirect effect of the bias on the default policy is bounded.





Discussion

TO BE ADDED

A Equilibrium Characterization: Baseline Model

The Policymaker's optimal policy as a function of her beliefs about w is E[w|m]+b/w. When the Policymaker observes the revealing message m = s, she implements policy

$$a^*(m=s) = m/2 + b/2.$$

Let $d^*(b, R)$ represent the default policy the Policymaker implements when $m = \emptyset$. Therefore, the Agency reveals observed signal s if and only if

$$-(a^*(m=s))^2 > -(d^*(b,R))^2.$$

Substituting for $a^*(m = s)$ and isolating s,

$$-2 \cdot d^*(b) - b < s < 2 \cdot d^*(b) - b.$$

Given the agency's revelation strategy, the posterior expectation of the state of the world after $m = \emptyset$ is

$$\int_{-\infty}^{-2 \cdot d^*(b) - b} x \cdot \phi(x) dx + \int_{2 \cdot d^*(b) - b}^{\infty} x \cdot \phi(x) dx$$
$$= \frac{1}{\sqrt{\pi}} \cdot (e^{-(b/2 - d)^2} - e^{-(b/2 + d)^2}),$$

where $\phi(\cdot)$ is the PDF of the standard normal distribution. Thus, the unique optimal default policy d the Policymaker implements after $m = \emptyset$ is implicitly defined by

$$d = b/2 + \frac{1}{\sqrt{\pi}} \cdot (e^{-(b/2-d)^2} - e^{-(b/2+d)^2}).$$
(11)

The solution to (11) is $d^*(b)$.

B Default Policy and Bias

The policy-maker's optimal choice of policy, given her posterior beliefs, is $\frac{E[w|\cdot]+b}{2}$. Let b > 0. Then d < b/2 only if $E[w|\emptyset] < 0$. Because w is symmetrically distributed around 0, $E[w|\emptyset] < 0$ only if $|\overline{s^*}(b)| > |\underline{s^*}(b)|$. Substituting from (3), this is equivalent to $2d^*(b) - b > 2d^*(b) + b$ or -b > b, a contradiction. Thus, for b > 0, d > b/2. By similar reasoning, b < 0 implies d < b/2.

C Default Policy as a Function of Bias

Without loss of generality, let us assume that the Policymaker exhibits a right-ward bias b > 0. Recall that the optimal default policy $d^*(b)$ is characterized by (11).

Let us denote the following function as F:

$$F \equiv d - b/2 - \frac{1}{\sqrt{\pi}} \cdot \left(e^{-(b/2 - d)^2} - e^{-(b/2 + d)^2}\right).$$
(12)

By the implicit function theorem

$$\partial_b d(\cdot) = -\frac{\partial_b F}{\partial_d F}.$$
(13)

We compute that

$$\partial_b F = -\frac{1}{2} - \frac{1}{\sqrt{\pi}} \cdot \left(e^{-(b/2-d)^2} \cdot (d-b/2) + e^{-(b/2+d)^2} \cdot (d+b/2) \right).$$
(14)

Because d^* exceeds b/2,

$$\partial_b F < 0. \tag{15}$$

At the same time,

$$\partial_d F = 1 - \frac{2}{\sqrt{\pi}} \cdot \left(-e^{-(b/2-d)^2} (d-b/2) + e^{-(b/2+d)^2} (d+b/2) \right).$$
(16)

Because for b > 0, the optimal default policy d^* exceeds b/2, it must be that

$$-\frac{2}{\sqrt{\pi}} \cdot \left(-e^{-(b/2-d)^2}(d-b/2) > 0\right)$$

. Therefore,

$$\partial_d F > 1 - \frac{2}{\sqrt{\pi}} \cdot e^{-(b/2+d)^2} (d+b/2).$$
 (17)

Note that $e^{-x^2}x$ reaches its maximum of $\frac{1}{\sqrt{2e}}$ at $x = \frac{1}{\sqrt{2}}$. Therefore $-\frac{2}{\sqrt{\pi}} \cdot e^{-(b/2+d)^2}(d+b/2)$ has a minimum value $-\frac{\sqrt{2}}{\sqrt{e\pi}}$, and thus for $d = d^*$, it must be that

$$\partial_d F > 1 - \frac{\sqrt{2}}{\sqrt{e \cdot \pi}} > 0. \tag{18}$$

Combining (13), (15), and (18), we obtain $\delta_b d(\cdot) > 0$.

D Impact of Bias on Agency's Strategy

D.1 Asymmetry in Revelation

Without loss of generality, let us assume that b > 0. Than $\overline{s^*}(b) = 2 \cdot d - b$ is less than $2 \cdot d + b = |\underline{s^*}(b)|$.

D.2 Asymmetry as a Function of Bias

Note that the difference between the range of revelation of positive signals and the range of revelation of negative ones increases as b increases:

$$\overline{s^*}(b) - |\underline{s^*}(b)| = 2 \cdot b,$$

where $2 \cdot b$ increases in b.

E Impact of Bias on Informativeness of Communication

Because the default policy increases in bias (Proposition 2), both the direct and the indirect effects of increasing bias on lower revelation thresholds are negative and thus the lower revelation threshold $\underline{s^*}(b)$ decreases in the Policymaker's bias.

Let us now consider upper revelation threshold. Without loss of generality, we assume b > 0. From (3),

$$\overline{s^*}(b) = 2 \cdot d^*(b) - b.$$

The derivative of the upper threshold with respect to b is

$$\frac{\partial \overline{s^*}(b)}{\partial b} = 2 \cdot \frac{\partial d^*(b)}{\partial b} - 1.$$
(19)

Substituting from (4),

$$\frac{\partial \overline{s^*}(b)}{\partial b} = \frac{\partial \left(\frac{2}{\sqrt{\pi}} \cdot \left(e^{-(b/2 - d^*(b))^2} - e^{-(b/2 + d^*(b))^2}\right)\right)}{\partial b}$$
$$= \frac{2}{\sqrt{\pi}} \cdot \left(e^{-(b/2 + d^*(b))^2} \cdot \left(d^*(b) + b/2\right) \cdot \left(2 \cdot \frac{\partial d^*(b)}{\partial b} + 1\right)\right)$$
$$-e^{-(b/2 - d^*(b))^2} \cdot \left(d^*(b) - b/2\right) \cdot \left(2 \cdot \frac{\partial d^*(b)}{\partial b} - 1\right)\right).$$

To establish the result by contradiction, let us assume that $\overline{s^*}(b)$ weakly decreases in b, and, thus, from (19) there is some point \hat{b} at which $2 \cdot \frac{\partial d^*(b)}{\partial b} - 1 \leq 0$. Then, at this point, $e^{-(b/2-d^*(b))^2} \cdot (d^*(b) - b/2) \cdot (2 \cdot \frac{\partial d^*(b)}{\partial b} - 1) \leq 0$ because $e^{-(b/2-d^*(b))^2}$ is always positive and, from (4), $d^*(b)$ exceeds b/2. But, then the sign of the derivative $\frac{\partial \overline{s^*}(b)}{\partial b}$ is strictly positive, which contradicts our initial assumption. Thus, upper threshold threshold always increases in b, and bias increases informativeness of communication.

F Coarse Partition of Signal Space

Consider a variation n the model in which the Agency's endowed language is coarser than the signal space. In particular, let there be a convex partition of the signal space into |M|intervals $(-\infty, \hat{m}_1), [\hat{m}_1, \hat{m}_2), ..., [\hat{m}_{|M|-1}, \infty)$. Associate a verifiable message with each of these intervals, where message m_j is available to the policy-maker iff $s \in [\hat{m}_j - 1, \hat{m}_j)$. Order the messages so that m_1 indicates the interval that includes $-\infty$ and m_M indicates the interval that includes $+\infty$. To simplify exposition, choose each m_i to satisfy $E[w|m_i] \equiv m_i$, i.e., $m_j = E[w|\hat{m}_{j-1} \leq s < \hat{m}_j]$. The Policy-maker can send the available verifiable message, given s, or $m = \emptyset$.

Proposition 9. Suppose that the Agency's possible actions include messages corresponding to exogenously given convex partitions of the signal space. Then the higher is the Policy-maker's bias (b), the more informative equilibrium communication between the Policymaker and the Agency becomes.

Proof. The Policy-maker chooses $a^*(m_i) = m_i \ \forall m_i \neq \emptyset$, and $a \ge d^*$ if $m = \emptyset$. The Agency, then, reveals a message m_i when

$$-d^* - b/2 < m_i < d^* - b/2, \tag{20}$$

and sends the message $m = \emptyset$ otherwise. Because all signals in the interval that corresponds to m_i result in the same policy choice, if the Agency prefers that policy choice to the default policy d^* , she will send m_i for all signals on that interval. For any two messages m_i and m_j such that $m_i < m_j$, if $-d^* - b/2 < m_i$ then $-d^* - b/2 < m_j$ and if $m_j < d^* - b/2$ then $m_i < d^* - b/2$. This implies that there will be greatest and least verifiable messages sent, and thus, upper and lower thresholds on the signals (imprecisely) revealed. Those thresholds will coincide, with, respectively, the lowest signal associated with the least and highest signal associated with the greatest of the verifiable messages the Agency reveals.

The default policy the Policymaker sets equals her posterior belief about the state of the

world upon observing $m = \emptyset$ plus her bias:

$$d^*(b) = E[w|m = \varnothing] + b/2.$$

From (20), the Agency reveals its information when

$$-E[w|m = \varnothing] - b < m_i < E[w|m = \varnothing].$$

Holding fixed the Policymaker's posterior, $E[w|m = \emptyset]$, suppose that the Policymaker's bias increases. Given b > 0, increasing b encourages the Agency to reveal more information on the side opposite of the Policymaker's bias. Returning to $E[w|m = \emptyset]$, note that because of the updated revelation strategy of the Agency, the Policymaker will form different beliefs about the state of the world conditional on a lack of revelation. In particular, the Policymaker will shift her belief in the direction of her bias (counteracting the Agency's effort to shift revelation in the opposite direction). But, then, as $E[w|m = \emptyset]$ increases, the Agency will be encouraged to reveal still more information, as the lack of revelation results in still more extreme default policy implementation.

G Equilibrium Characterization: Office Benefit

As in the main model, when the Policymaker observes a revealing message m = s, she implements policy $a^*(m = s) = m/2 + b/2$; R affects neither her beliefs nor her optimal policy choice when m = s. However, R may affect the range of signals that the Agency reveals, and hence the Policymaker's beliefs and actions following $m = \emptyset$. Let $d^*(b, R)$ represent the default policy the Policymaker implements after $m = \emptyset$. The Agency reveals its signal s if s is such that

$$-(a^*(m))^2 + R > -(d^*(b, R))^2.$$

Substituting for $a^*(m)$ and isolating s, we get

$$-2 \cdot \sqrt{R + d^*(b, R)^2} - b < s < 2 \cdot \sqrt{R + d^*(b, R)^2} - b.$$
(21)

Given the agency's revelation strategy, the posterior expected value of the state of the world after the agency chooses $m = \emptyset$ is

$$\int_{-\infty}^{-2 \cdot \sqrt{R+d^*(b,R)^2} - b} x \cdot \phi(x) dx + \int_{2 \cdot \sqrt{R+d^*(b,R)^2} - b}^{\infty} x \cdot \phi(x) dx$$

$$= \frac{1}{\sqrt{\pi}} \cdot \left(e^{-(b/2 - \sqrt{R+d^2})^2} - e^{-(b/2 + \sqrt{R+d^2})^2} \right),$$
(22)

where $\phi(\cdot)$ is PDF of standard normal distribution. The only sequentially rational policy after $m = \emptyset$ is d solving

$$d = b/2 + \frac{1}{\sqrt{\pi}} \cdot \left(e^{-(b/2 - \sqrt{R+d^2})^2} - e^{-(b/2 + \sqrt{R+d^2})^2}\right);$$
(23)

the solution is $d^*(b, R)$.

H Effect of Office Benefit on Informativeness of Communication

Part 1.

Let b > 0. From (7), the upper revelation threshold increases, and the lower revelation threshold decreases, in the office benefit R if and only if $(1 + 2 \cdot d \cdot \frac{\partial d^*(\cdot, R)}{\partial R})$ exceeds zero. To prove that it always exceeds zero, let us note that

$$\frac{\partial d^*(\cdot, R)}{\partial R} = \frac{1}{\sqrt{\pi}} \cdot \frac{1}{\sqrt{R+d^2}} \cdot (1+2 \cdot d \cdot \frac{\partial d^*(\cdot, R)}{\partial R})$$
(24)

$$\cdot \left(e^{-(\sqrt{R+d^2}+b/2)^2} \cdot (\sqrt{R+d^2}+b/2) - e^{-(\sqrt{R+d^2}-b/2)^2} \cdot (\sqrt{R+d^2}-b/2)\right).$$

Let $E := \left(e^{-(\sqrt{R+d^2}+b/2)^2} \cdot (\sqrt{R+d^2}+b/2) - e^{-(\sqrt{R+d^2}-b/2)^2} \cdot (\sqrt{R+d^2}-b/2)\right)$. Then, by the implicit function theorem,

$$\frac{\partial d^*(\cdot, R)}{\partial R} = \frac{\frac{1}{\sqrt{\pi}} \cdot \frac{1}{\sqrt{R+d^2}} \cdot E}{1 - 2 \cdot \frac{d}{\sqrt{R+d^2}} \cdot \frac{1}{\sqrt{\pi}} \cdot E}.$$
(25)

First consider the case E < 0. Then, from (25):

$$\frac{\partial d^*(\cdot, R)}{\partial R} = \frac{\frac{1}{\sqrt{\pi}} \cdot \frac{1}{\sqrt{R+d^2}} \cdot E}{1 - 2 \cdot \frac{d}{\sqrt{R+d^2}} \cdot \frac{1}{\sqrt{\pi}} \cdot E} > -\frac{1}{2 \cdot d},\tag{26}$$

where the last inequality follows because, from Lemma 1 and b > 0, d > 0. This implies

$$1 + 2d\frac{\partial d^*(\cdot, R)}{\partial R} > 0.$$
⁽²⁷⁾

and, thus, that the upper revelation threshold increases, and the lower revelation threshold decreases, in the office benefit R.

Now consider the case E > 0. Because $e^{-(\sqrt{R+d^2}-b/2)} \cdot (\sqrt{R+d^2}-b/2) > 0$,

$$1 - 2 \cdot \frac{d}{\sqrt{R+d^2}} \cdot \frac{1}{\sqrt{\pi}} \cdot \left(e^{-(\sqrt{R+d^2}+b/2)^2} \cdot (\sqrt{R+d^2}+b/2) - e^{-(\sqrt{R+d^2}-b/2)} \cdot (\sqrt{R+d^2}-b/2)\right) \\ > 1 - 2 \cdot \frac{d}{\sqrt{R+d^2}} \cdot \frac{1}{\sqrt{\pi}} \cdot e^{-(\sqrt{R+d^2}+b/2)^2} \cdot (\sqrt{R+d^2}+b/2).$$
(28)

Because $\frac{d}{\sqrt{R+d^2}} < 1$,

$$1 - 2 \cdot \frac{d}{\sqrt{R+d^2}} \cdot \frac{1}{\sqrt{\pi}} \cdot e^{-(\sqrt{R+d^2}+b/2)^2} \cdot (\sqrt{R+d^2}+b/2) > 1 - 2 \cdot \frac{1}{\sqrt{\pi}} \cdot e^{-(\sqrt{R+d^2}+b/2)^2} \cdot (\sqrt{R+d^2}+b/2) > 1 - \frac{\sqrt{2}}{\sqrt{e\cdot\pi}},$$
(29)

where the last inequality follows because xe^{-x} has a maximum of $\frac{1}{\sqrt{2e}}$. Because $1 - \frac{\sqrt{2}}{\sqrt{e \cdot \pi}} > 0$, the denominator of the RHS of (25) is positive. Given E > 0, the numerator of RHS of (25) is also greater than 0, and so $\frac{\partial d^*(\cdot,R)}{\partial R} > 0$. Thus, $(1 + 2 \cdot d \cdot \frac{\partial d^*(\cdot,R)}{\partial R})$ exceeds zero and the upper revelation threshold increases, and the lower revelation threshold decreases, in the office benefit.

Part 2.

We must establish that $\underline{s}^*(b, R)$ is decreasing in b and that $\overline{s}^*(b, R)$ is increasing in b. Both direct and indirect effects of an increase in b on $\underline{s}^*(b, R)$ are negative; thus $\underline{s}^*(b, R)$ is decreasing in b. From (7),

$$\frac{\partial \overline{s^*}(b,R)}{\partial b} = \frac{2d^*(b,R)}{\sqrt{R+d^*(b,R)^2}} \frac{d^*(b,R)}{\partial b} - 1.$$
(30)

Requiring that this be positive yields an inequality equivalent to (9).

I Office Benefit Unique Threshold

Note that when R = 0, $\overline{s^*}(b, R = 0) > \overline{s^*}(b = 0, R = 0)$. When R, instead, converges to infinity, d converges to b/2, and $\overline{s^*}(b, R = \infty) < \overline{s^*}(b = 0, R = \infty)$. Because both are continuous, it implies that there will exist a threshold R^* s.t., for all $R < R^*$, the Agency reveals strictly more information to the biased Policymaker than to the unbiased one.

J Agency's Revelation and Agency's Conservatism

WLOG, we assume b > 0. Let us note that the Agency reveals information to the Policymaker when

$$\begin{cases} c < 1/2, \ m \in (-\infty, \ 2 \cdot d^* - b] \cup [\frac{2 \cdot d^* + b}{1 - 2 \cdot c}, \ +\infty), \\ c \ge 1/2, \ m \in [\frac{2 \cdot d^* + b}{1 - 2 \cdot c}, \ 2 \cdot d^* - b], \end{cases}$$

where d^* solves

$$d = b/2 + \frac{1}{\sqrt{\pi}} \cdot \left(e^{-(b/2-d)^2} - e^{-\frac{(b/2+d)^2}{(1-2\cdot c)^2}}\right).$$

Let us denote as $F_1 \equiv d - b/2 - \frac{1}{\sqrt{\pi}} \cdot \left(e^{-(b/2-d)^2} - e^{-\frac{(b/2+d)^2}{(1-2\cdot c)^2}}\right).$

Note that the default function's derivative with respect to c is equal to

$$\frac{\partial d(c,\cdot)}{\partial c} = -\frac{\frac{\partial F_1(c,d,\cdot)}{\partial c}}{\frac{\partial F_1(c,d,\cdot)}{\partial d}},$$

where

$$\begin{aligned} \frac{\partial F_1(c,d,\cdot)}{\partial d} &= 1 - \frac{2}{\sqrt{\pi}} \cdot \left(-e^{-(b/2-d)^2} \cdot (d-b/2) + e^{-(b/2+d)^2/(1-2\cdot c)^2} \cdot \frac{b/2+d}{(1-2\cdot c)^2} \right) \\ &> 1 - \frac{2}{\sqrt{\pi}} \cdot e^{-(b/2+d)^2/(1-2\cdot c)^2} \cdot \frac{b/2+d}{(1-2\cdot c)^2} \\ &> 1 - \frac{2}{\sqrt{\pi}} \cdot e^{-(b/2+d)^2} \cdot (b/2+d) \\ &> 1 - \frac{\sqrt{2}}{\sqrt{e\cdot\pi}}. \end{aligned}$$

Therefore,

$$sgn(\frac{\partial d(c,\cdot)}{\partial c}) = -sgn(\frac{\partial F_1(c,d,\cdot)}{\partial c}).$$

Because

$$\frac{\partial F_1(c,d,\cdot)}{\partial c} = -\frac{(b+2\cdot d)^2 \cdot e^{-\frac{(b/2+d)^2}{(1-2\cdot c)^2}}}{(1-2\cdot c)^3 \cdot \sqrt{\pi}},$$

the optimal default policy d^* increases in c when c<1/2 and decreases in c when $c\geq 1/2.$ Finally, when c<1/2

$$\frac{\partial \frac{b+2\cdot d}{1-2\cdot c}}{\partial c} > \frac{\partial (2\cdot d-b)}{\partial c}.$$

Therefore, the Agency's revelation strictly decreases in the Agency's conservatism.

Let us now consider how Policymaker's bias affects the Agency's revelation for different

levels of the Agency's conservatism. Because $\frac{\partial F(c,d,\cdot)}{\partial d} > 0$,

$$sgn(\frac{\partial d(b,\cdot)}{\partial b}) = -sgn(\frac{\partial F_1(b,d,\cdot)}{\partial b}).$$

$$\begin{aligned} \frac{\partial F_1(b,d,\cdot)}{\partial b} &= -1/2 + \frac{1}{\sqrt{\pi}} \cdot \left(e^{-(b/2-d)^2} \cdot (b/2-d) \cdot 1/2 - e^{-\frac{(b/2+d)^2}{(1-2\cdot c)^2}} \cdot (b/2+d) \cdot 1/2 \right) \\ &= -1/2 - \frac{1}{\sqrt{\pi}} \cdot e^{-(b/2-d)^2} \cdot (d-b/2) \cdot 1/2 - \frac{1}{\sqrt{\pi}} \cdot e^{-\frac{(b/2+d)^2}{(1-2\cdot c)^2}} \cdot (b/2+d) \cdot 1/2 < 0. \end{aligned}$$

Therefore, the optimal default policy $d^*(b, \cdot)$ increases in the Policymaker's bias b.

The Agency reveals signal to the Policymaker when

$$\begin{cases} c < 1/2, \ m \le 2 \cdot d^* - b \ or \ m \ge \frac{2 \cdot d^* + b}{1 - 2 \cdot c}, \\ c \ge 1/2, \ \frac{2 \cdot d^* + b}{1 - 2 \cdot c} \le m \le 2 \cdot d^* - b. \end{cases}$$

 $\frac{2 \cdot d^* + b}{1 - 2 \cdot c} \text{ increases in } b \text{ when } c < 1/2 \text{ and decreases in } b \text{ otherwise. Finally, because } Abs(\frac{\partial (2 \cdot d^* - b)}{\partial b}) < Abs(\frac{\partial \frac{2 \cdot d^2 + b}{1 - 2 \cdot c}}{\partial b}), \text{ communication increases in bias when } c > 1/2 \text{ and decreases in bias otherwise.}$

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